

## AP Calc AB Ch 2 Review 2

- \*p.107 know how to work with “e” the natural base
- \*know how to find:
  - limits
  - slopes of tangents
- \*know the squeeze theorem p.85 #35, 36
- \*p.95 #3-4
- \*find the average rate of change over a time interval (like quiz)
- \*write the equation of a TANGENT and a NORMAL to a curve at an x-value
- \*know IVT similar to p.107 47-52, p.109 27-28, know how to use calc to find zeros
- \*know how to graph with greatest integer, p.109 #30, p.86 49-51
- \*be able to find a point of discontinuity
- \*be able to look at a graph and determine if continuous and where it is continuous
- \*be able to find ave velocity and instantaneous velocity
- \*#1 on first review...be able to look at graphs and determine limits
- \*p.107 #41, study the one we did in notes for section 2.5

### Sample Problems

Calc OK

1. If  $1-x^4 \leq f(x) \leq 1 + 2x^2$ , find the  $\lim_{x \rightarrow 0} f(x)$
2. Find the average rate of change of  $f(x) = 1 - x^4$  over  $[-1, 4]$ .
3. Write the equation of the tangent to  $f(x) = 2x^2 - 3$  at  $x = 1$ . What is the equation of the normal to this?
4. Use IVT to show that  $x^5 - 6x^2 + 2x + 1$  has at least 1 solution. Next, find all real solutions.
5. Graph  $f(x) = \llbracket x \rrbracket + 2$  on  $-5 \leq x \leq 5$

NO Calc

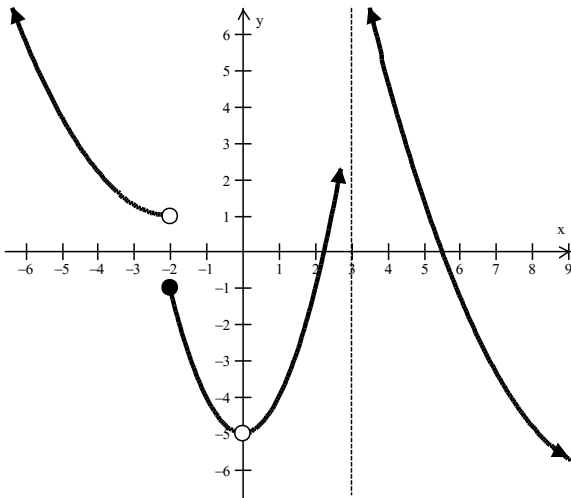
1. Let  $f(x) = 3x^2 - 5x$  and P the point  $(2, 2)$ . Find the slope, the equation of tangent and equation of normal to  $f(x)$  at P.

$$2. f(x) = \begin{cases} a - x^2 & x \leq 1 \\ 2x & x > 1 \end{cases}$$

- a) find  $\lim_{x \rightarrow 1^-} f(x)$       b) find  $\lim_{x \rightarrow 1^+} f(x)$       c) Find all values of a that make f continuous at 1.

3.

Below is the graph of  $f(x)$

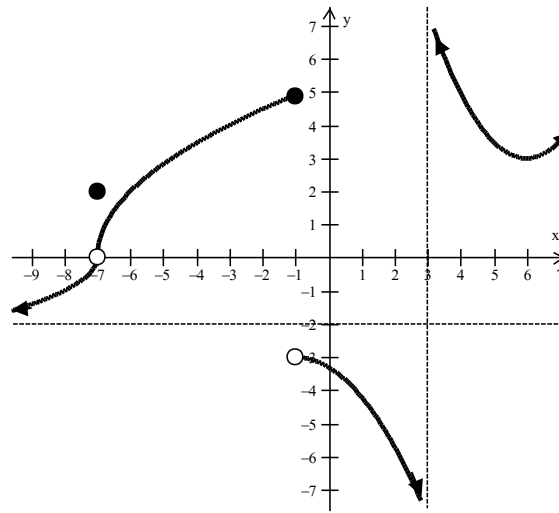


$$\lim_{x \rightarrow -\infty} f(x) =$$

$$\lim_{x \rightarrow \infty} f(x) =$$

4.

Below is the graph of  $g(x)$



$$\lim_{x \rightarrow -\infty} g(x) =$$

$$\lim_{x \rightarrow \infty} g(x) =$$

$$\lim_{x \rightarrow -2^-} f(x) =$$

$$\lim_{x \rightarrow -2^+} f(x) =$$

$$\lim_{x \rightarrow -2} f(x) =$$

$$\lim_{x \rightarrow -7^-} g(x) =$$

$$\lim_{x \rightarrow -7^+} g(x) =$$

$$\lim_{x \rightarrow -7} g(x) =$$

$$\lim_{x \rightarrow 0^-} f(x) =$$

$$\lim_{x \rightarrow 0^+} f(x) =$$

$$\lim_{x \rightarrow 0} f(x) =$$

$$\lim_{x \rightarrow -1^-} g(x) =$$

$$\lim_{x \rightarrow -1^+} g(x) =$$

$$\lim_{x \rightarrow -1} g(x) =$$

$$\lim_{x \rightarrow 3^-} f(x) =$$

$$\lim_{x \rightarrow 3^+} f(x) =$$

$$\lim_{x \rightarrow 3} f(x) =$$

$$\lim_{x \rightarrow 3^-} g(x) =$$

$$\lim_{x \rightarrow 3^+} g(x) =$$

$$\lim_{x \rightarrow 3} g(x) =$$

On what intervals is  $f(x)$  is continuous? On what intervals is  $g(x)$  is continuous?

5. Use the graphs above to find:

a) find  $\lim_{x \rightarrow 2} [f(x) \cdot g(x)]$

b) find  $\lim_{x \rightarrow 2} \frac{g(x)}{f(x)}$

c) find  $\lim_{x \rightarrow -7} x + g(x)$

6. The table below shows several measurements of the velocity of motorcycle driving on a straight road.  $v(t)$  is continuous on the interval  $[3, 17]$ .

$t$ (min)	3	5	7	11	13	17
$v(t)$ (meters/min)	221.7	321.4	457.8	563.9	421.5	297.2

What is the least number of times where  $v(t)$  is exactly 325 meters/min? Justify your answer.