## AP Calculus Chapter 4 Test 2 Review 2

1. Suppose you have the graph of $f^{\prime}(x)$ to be:
a) Where is $f(x)$ increasing and concave down?
b) Where is $f(x)$ increasing at an increasing rate?

2. Given the following table of values for $t$ in seconds and $v(t)$ in meters per second:

| t | 2 | 4 | 6 | 8 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{v}(\mathrm{t})$ | -3 | 2 | 5 | 7 | 12 |

Estimate a(5)
3. Given the following line graph for $f^{\prime}(x)$
a) What are the critical points?

b) Where is there a relative maximum/minimum for $f(x)$ ? Justify your reasoning.
c) Where is $f(x)$ increasing/decreasing? Justify your reasoning.
4. Given the following equation: $\quad f(x)=x^{3}-6 x^{2}+12 x$
a) Find all relative extrema.
b) Find all inflection points.
c) Find all values of $c$ that are guaranteed by MVT on [0, 4]
5. Use the table below to sketch a graph of the function $f(x)$.

| x | $(-\infty,-2)$ | -2 | $(-2,-1)$ | -1 | $(-1,2)$ | 0 | $(2,4)$ | 4 | $(4, \infty)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| f |  | 0 |  | DNE |  | 0 |  | 6 |  |
| $\mathrm{f}^{\prime}$ | + |  | + |  | + |  | + | DNE | + |
| $\mathrm{f}^{\prime \prime}$ | + |  | + |  | - |  | + |  | + |

6. Suppose you have 80 linear feet of fencing to enclose a rectangular space for a garden. Find the largest possible area that can be enclosed with this much fencing. What are the dimensions that yield this area?
7. Squares of equal sides are cut of a $20 \times 24$ rectangle and folded up to form a box with an open top. What are the dimensions of the squares to form the largest possible volume?
8. Find the antiderivative of each of the following:
a) $f^{\prime}(x)=2 x^{3}-5 x^{2}-3 x+2$
b) $f^{\prime}(x)=\cos x-2 \sec ^{2} x$
