Find the area bounded by each curve.

1. $y=\sqrt[3]{x}$ and $y=\sqrt{x}$
2. $y=\sqrt[3]{x-3}$ and $y=13-x$
3. $x=2 y^{2}-2 y$ and $x=12 y^{2}-12 y^{3}$

Find the volume of the solid bounded by:
4. $y=x^{2}, y=0$ and $x=2$ revolved about the $x$-axis.
5. $y=2 x-x^{2}$ and $y=x$ about $y=1$.
6. $y=\frac{x^{2}}{4}$ and $y=1$ about the line $y=2$.
7. $y=4-x^{2}$ and $y=0$ about the line $y=-3$
8. $y=2 \sqrt{x-1}$ and $y=x-1$ about the line $x=-1$

