

AP Calc Chapter 7 Review – All

Find the limit of each. Use L'Hopital if needed.

$$1. \lim_{x \rightarrow 0} \frac{\sin 3x}{\sin 4x}$$

$$2. \lim_{x \rightarrow 0} \frac{x - \sin x}{x^3}$$

$$3. \lim_{x \rightarrow \infty} \frac{5x^3 - 4x^2 + 1}{7x^3 + 2x - 6}$$

$$4. \lim_{x \rightarrow \infty} x e^{-2x}$$

Find the derivative of each.

$$5. y = \ln^3 x$$

$$6. f(x) = \frac{x^2}{\ln x}$$

$$7. y = 3^{-2x}$$

$$8. f(x) = \sin^{-1}(2x)$$

$$9. f(x) = 3\arccos(5x)$$

$$10. f(x) = 4^{x-5}$$

Integrate each.

$$11. \int \frac{4}{\sqrt{25-x^2}} dx$$

$$12. \int \frac{1}{36+4x^2} dx$$

$$13. \int x e^{3x^2+1} dx$$

$$14. \int 6^x dx$$

$$15. \int \frac{e^x}{1+e^x} dx$$

$$16. \text{Find } (f^{-1})'(a) \text{ for } f(x) = \frac{2}{x} - e^x \text{ at } a = 1.$$

17. The waitress pours coffee into your cup at 10:00 am. The coffee is 180° when freshly poured and after 2 minutes in a room at 70°F , the coffee has cooled to 165°F . Find the temperature at any time t and find the time at which the coffee is 120°F .